Attenuation of Blood Flow Pulsatility along the Atlas Slope: A Physiologic Property of the Distal Vertebral Artery?

T. Schubert, M. Pansini, O. Bieri, C. Stippich, S. Wetzel, S. Schaedelin, A. von Hessling, and F. Santini

ABSTRACT

BACKGROUND AND PURPOSE: Physiologic and pathologic arterial tortuosity may attenuate blood flow pulsatility. The aim of this prospective study was to assess a potential effect of the curved V3 segment (Atlas slope) of the vertebral artery on arterial flow pulsatility. The pulsatility index and resistance index were used to assess blood flow pulsatility.

MATERIALS AND METHODS: Twenty-one healthy volunteers (17 men, 4 women; mean age, 32 years) were examined with a 3T MR imaging system. Blood velocities were measured at 2 locations below (I and II) and at 1 location above the V3 segment (III) of the vertebral artery by using a high-resolution 2D-phase-contrast sequence with multidirectional velocity-encoding.

RESULTS: Pulsatility and resistance indices decreased along all measurement locations from proximal to distal. The pulsatility index decreased significantly from location II to III and from I to II. However, the decrease was more pronounced along the Atlas slope than in the straight-vessel section below. The decrease of the resistance index was highly significant along the Atlas slope (location II to III). The decrease from location I to II was small and not significant.

CONCLUSIONS: The pronounced decrease in pulsatility and resistance indices along the interindividually uniformly bent V3 segment compared with a straight segment of the vertebral artery indicates a physiologic attenuating effect of the Atlas slope on arterial flow pulsatility. A similar effect has been described for the carotid siphon. A physiologic reduction of pulsatility in brain-supplying arteries would be in accordance with several recent publications reporting a correlation of increased arterial flow pulsatility with leukoencephalopathy and lacunar stroke.

ABBREVIATIONS: PC = phase-contrast; PI = pulsatility index; RI = resistance index; Vmax = maximum blood velocity; Vmean = mean blood velocity; Vmin = minimum blood velocity

The flow waveform in an arterial vessel is affected by many factors. Main influencing parameters are inflow determinants (cardiac function), outflow determinants (downstream tissue), and resistance presented by the vessel wall.¹⁻⁴

Due to the different functions of large and small arteries, arterial flow waveforms undergo changes along the vascular tree. The large conduit arteries have an elastic wall to minimize longitudinal impedance.⁵ In contrast, the distal arteries that regulate the demand for blood of the downstream tissue have a more muscular wall to effectively change lumen size.

The elasticity of the large arteries has a buffering function, which decreases pressure and flow pulsatility by taking up energy during systole and releasing it during diastole (Windkessel effect), thus delivering blood in a more continuous stream to peripheral vascular beds.⁶ Due to increased wall stiffness, waveform changes occur with normal aging but also in pathologies that affect vascular compliance.⁷ Recent studies with large patient cohorts indicate that the brain is vulnerable to increased arterial pulsatility, reflected by a higher number of white matter hyperintensities and a greater incidence of lacunar strokes.⁸⁻¹⁰

The most important techniques for noninvasive flow measurements and therefore flow wave characterization are Doppler sonography and phase-contrast (PC) MR imaging. Both techniques are important clinical tools. Doppler sonography has the advantage of a widely available method with very high spatial and temporal resolution; however, it is user-dependent and restricted to sonography-accessible vessel locations.¹¹ Phase-contrast MR imaging, in turn, has the advantage of providing blood flow measurements independent of the user without an-

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From the Divisions of Neuroradiology (T.S., C.S., A.v.H.) and Radiological Physics (O.B., F.S.), Clinic of Radiology and Nuclear Medicine, and Clinical Trial Unit (S.S.), Basel University Hospital, Basel, Switzerland; Department of Radiology (M.P.), Bruderholz Cantonal Hospital, Basel, Switzerland; and Department of Neuroradiology (S.W.), Hirslanden Clinic, Zurich, Switzerland.

Please address correspondence to Tilman Schubert, MD, Division of Neuroradiology, Clinic of Radiology and Nuclear Medicine, Basel University Hospital, Petersgraben 4, 4031 Basel, Switzerland; e-mail: Tilman.Schubert@usb.ch

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atomic restrictions, however, with lower spatial and temporal resolution.¹²⁻¹⁴

Regarding PC-MR imaging, a 2D-PC sequence with unidirectional velocity-encoding is routinely applied. This sequence is fast and robust; however, due to its unidirectional vessel encoding, it may underestimate flow velocities due to placement errors.¹⁵ Newer techniques such as 4D-PC-MR imaging and 2D-PC-MR imaging with multidirectional velocity-encoding have been shown superior to 2D-PC-MR imaging with unidirectional velocity-encoding in curved vessel sections.¹⁶⁻¹⁹

The aim of the present study was to evaluate blood flow characteristics along the curved vessel section of the distal vertebral artery, extending from the transverse foramen C2 to the dura mater cranial to the Atlas vertebra (Atlas slope), to evaluate the effect of a tortuous vessel geometry on blood flow pulsatility. For blood flow and velocity measurements, a

2D-PC sequence with multidirectional velocity-encoding has been applied.

MATERIALS AND METHODS

Study Population

Forty-two vertebral arteries of 21 healthy volunteers without pre-existing conditions (17 male; mean age, 32 ± 5.2 years; range, 23–40 years) were prospectively investigated.

For each vessel, time-resolved measurements of blood velocities and flow volume were acquired at 2 locations below (location I, level of the cervical vertebral body 6; location II, level of the upper cervical vertebral body 3 immediately below the Atlas slope) and at 1 location above the V3 segment (location III, intradural V4 segment) of the vertebral artery (Fig 1). The study was approved by the local ethics review committee, and written informed consent was obtained from all subjects.

MR Imaging Measurements

Data were acquired on a 3T MR imaging system (Magnetom Verio; Siemens, Erlangen, Germany). After localizer measurements, a time-of-flight angiography was used to identify the vertebral artery segments and to plan the subsequent velocity-encoded acquisitions. The velocity-encoded MR imaging consisted of *k*-space segmented 2D radiofrequency-spoiled gradient-echo sequences with prospective electrocardiography gating and interleaved 3-directional velocity-encoding. The applied 2D-PC acquisition with 3D-velocity-encoding used a $187 \times 151 \text{ mm}^2$ rectangular FOV and a spatial resolution of $0.5 \times 0.5 \times 5 \text{ mm}^3$. Data acquisition resulted in a series of datasets representing the components of the velocity vector in consecutive timeframes within the cardiac cycle with a temporal resolution of 68 ms. The total acquisition times were approximately 90 seconds with variability depending on the patient's individual heart rate (10–16 acquired cardiac cycles). Velocity-encoding sensitivity was 80 cm/s along all 3 encoding directions. Further imaging parameters were the following: TR/TE, 8.5/5.7 ms; flip angle, 30°; bandwidth, 460 Hz/pixel. The velocity distributions for each voxel and time point within the cardiac cycle were reconstructed from data acquired over numerous cardiac cycles throughout the total acquisition period.

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Postprocessing

Semiautomated postprocessing of the datasets was performed by using an in-house software tool developed with Matlab (MathWorks, Natick, Massachusetts) for the definition of ROIs based on manual region selection and signal thresholding of the magnitude images.²⁰⁻²²

Outcome Measures

Minimum and maximum velocities were extracted from individual flow-velocity curves (Fig 2). Mean velocity was calculated by dividing the sum of velocities by the time points.

FIG 1. Measurement locations along the vertebral artery (I–III) depicted on a contrast-enhanced MRA (left) and on a schematic image in relation to the bony anatomy (right).

FIG 2. Depiction of a flow-velocity waveform with the calculated mean velocity indicated. X-axis: centimeters per second; Y-axis: cardiac phases.

Table 1: Measured velocities at locations I–III

Variable	Mean	Median	Minimum	Maximum	SD
Vmin I	13.3	12.7	8.4	21.6	3.0
Vmax I	39.3	40	27.8	52.5	6.7
Vmean I	23	22.4	15.7	30.8	4.1
Vmin II	12.6	12.4	5.6	21.2	3.5
Vmax II	36.3	36.5	18.5	55	6.7
Vmean II	23.9	24.3	10.2	34.2	5
Vmin III	17.4	16.9	8.9	32.9	4.8
Vmax III	41	37.8	19.4	72.6	10.4
Vmean III	29.7	28.9	14	52.9	7.2

Table 2: Descriptive characterization of the parameters PI and RI

Variable	Mean	SD
PI I	1.15	0.22
PI II	1.01	0.18
PI III	0.79	0.13
RI I	0.66	0.06
RI II	0.65	0.07
RI III	0.57	0.07

For quantification of pulsatility, the pulsatility index (PI) and resistance index (RI) were applied.

The pulsatility index and resistance index were calculated according to the following formulas by using blood velocities^{23,24}:

$$\text{Pulsatility Index: PI} = \frac{V_{\max} - V_{\min}}{V_{\text{mean}}},$$

$$\text{Resistance Index: RI} = \frac{V_{\max} - V_{\text{enddiastolic}}}{V_{\max}}.$$

Statistical Analysis

Both end points, PI (primary end point) and RI, were calculated for the left and right vertebral arteries at the 3 locations (I, II, and III) as described above for 21 healthy volunteers:

For the end points PI and RI and for minimum blood velocity (Vmin), maximum blood velocity (Vmax), and mean blood velocity (Vmean), a linear mixed-effects model was fit with segment location as mixed-effect, and volunteer and side (nested within volunteer), as random effects for which separate intercepts were fit. The significance of mixed-effects was calculated by using a *t* test with Satterthwaite approximation for *df*.

RESULTS

Pulsatility and Resistance Indices

Calculation of Indices. Vmin was invariably found before the systolic upstroke of the flow curve; therefore, Vmin conformed to blood velocity at end of diastole in our measurements, which was then used to calculate the resistance index.

In general, the mean values for PI and RI decreased from proximal to distal. Both PI and RI showed a pronounced decrease between the segments II and III (Tables 1 and 2).

Table 3 shows the descriptive statistics for the parameters PI and RI. Boxplots of the indices are given in Figs 3 and 4.

Table 3: Estimates and confidence interval for the mixed-effect “location” and the end point pulsatility index^a

	Estimate	SD	95% CI	T	P
(Intercept)	1.01	0.03	(0.9–1.07)	33.8	<.001
I	0.14	0.03	(0.08–0.2)	4.67	<.001
III	–0.22	0.03	(–0.27–0.16)	–7.42	<.001

^a Location II is taken as base. This means that the estimate of the decrease from I (respectively III) to II is calculated by comparing the pulsatility index at segment I (respectively III) with the pulsatility index at segment II (Intercept), which explains the negative sign for the estimate in sections II to III. The estimated variances between volunteers and those between left and right side measurements are negligible.

FIG 3. Boxplots of pulsatility indices per location on both sides. **FIG 4.** Boxplots of resistance indices per location on both sides.**Table 4: Estimates and confidence interval for the mixed-effect “location” and the end point resistance index^a**

	Estimate	SD	95% CI	T	P
(Intercept)	0.65	0.01	(0.63–0.67)	59.16	<.001
I	0.007	0.012	(–0.02–0.03)	0.61	0.54
III	–0.08	0.012	(–0.1 to –0.05)	–6.54	<.001

^a Location II is taken as base. This means that the estimate of the decrease from I (respectively III) to II is calculated by comparing the pulsatility index at segment I (respectively III) with the pulsatility index at segment II (Intercept), which explains the negative sign for the estimate in sections II to III. The estimated variances between volunteers and those between left and right side measurements are negligible.

Pulsatility Index

The pulsatility index median was lower at the distal segment III than at the proximal segments I and II (Fig 3). According to the results of the mixed-effects models (Table 3), the decrease of PI was highly significant from II to III and from I to II, but the effect size was much higher in the section between II and III (average decrease of 0.22) than in the section between I and II (average decrease of 0.14).

The estimated variances between volunteers and left and right side measurements were negligible.

Resistance Index: Model

The resistance index median was lower at distal segment III than at proximal segments I and II (Fig 4). According to the results of the mixed-effects models (Table 4), the decrease of RI was highly significant from segments II to III (average decrease of 0.08). The

Table 5: Estimates and confidence interval for the fixed-effect "location" and the end point minimal blood velocity^a

	Estimate	SD	95% CI	T	P
(Intercept)	12.6067	0.59	(11.44–13.78)	21.24	<0.001
I	0.81	0.57	(–0.32–1.94)	1.4	0.16
III	4.75	0.56	(3.64–5.86)	8.4	<0.001

^a Location II is taken as base. This means that the estimate of the increase/decrease from I (respectively III) to II is calculated by comparing the blood velocity at segment I (respectively III) with the blood velocity at segment II (Intercept).

Table 6: Estimates and confidence interval for the fixed-effect "location" and the end point mean velocity^a

	Estimate	SD	95% CI	T	P
(Intercept)	23.85	0.86	(22.15–25.55)	27.47	<0.001
I	–0.67	0.80	(–2.26–0.9)	–0.84	0.4
III	5.87	0.79	(4.32–7.43)	7.41	<0.001

^a Location II is taken as base. This means that the estimate of the increase/decrease from I (respectively III) to II is calculated by comparing the mean velocity at segment I (respectively III) with the mean velocity at segment II (Intercept).

Table 7: Estimates and confidence interval for the fixed-effect "location" and the end point maximum velocity^a

	Estimate	SD	95% CI	T	P
(Intercept)	36.32	1.26	(33.84–38.8)	28.68	<0.001
I	3.31	1.3	(0.76–5.86)	2.55	0.013
III	4.69	1.27	(2.19–7.2)	3.67	<0.001

^a Location II is taken as base. This means that the estimate of the increase/decrease from I (respectively III) to II is calculated by comparing the maximum velocity at segment I (respectively III) with the maximum velocity at segment II (Intercept).

decrease from segments I to II was small and not significant ($P = <.001$).

The estimated variances between volunteers and left- and right-side measurements were negligible.

Peak Velocities: Model

Minimum Velocity. According to the mixed-effects model results in Table 5, the increase in minimal velocity was highly significant from segments II to III. A decrease was found between segments I and II. Due to small effect size, this decrease was not significant.

Mean Velocity. According to the mixed-effects model results in Table 6, the increase in mean velocity is highly significant from segments II to III. A small increase was found between segments I and II. Due to small effect size, this increase was not significant.

Maximum Velocity. According to the mixed-effects model results in Table 7, the increase in minimal blood velocity is highly significant from segments II to III. A significant decrease was found between segments I and II.

Blood velocities per location are summarized in Table 1; box-plots are shown in Fig 5.

DISCUSSION

The main finding of the present study is a highly significant reduction of arterial flow pulsatility along the upper part of the vertebral artery, the Atlas slope.

The measured blood velocities (V_{min} , V_{max} , and V_{mean}) and indices (PI, RI) showed a nonlinear behavior along the 3 measurement locations (Fig 5). From segments I to II, only V_{max} showed a significant change (decrease), reflected by the decrease in RI. From segments II to III, all velocities increased significantly. However, V_{min} and V_{mean} increased relatively more strongly compared with V_{max} .

How the velocities changed along the vessel course was reflected by a clearly higher decrease of PI from locations II to III than from I to II. RI, in turn, stayed almost constant from locations I to II and showed a strong decrease from locations II to III, which indicates a greater effect on flow pulsatility of the Atlas slope compared with the straight-vessel section below.

The pulsatility index and resistance index are mainly used to describe the arterial resistance of a downstream capillary bed²⁵ and upstream vessel stenoses.²⁶ However, it is known that vascular compliance can also affect these indices.^{6–9} In our study, we measured blood velocities under the same circumstances of the downstream capillary bed at relatively close locations along the vertebral artery. Therefore, changes in PI and RI were most likely induced by the local vessel properties.

FIG 5. Boxplots of blood velocities per location on both sides.

The distinct reduction in flow pulsatility appeared along a geometrically complex, tortuous vessel section with high interindividual uniformity. The main function of this physiologic elongation of the vertebral artery is to provide the high range of motion of the upper cervical spine. However, the characteristic shape of the Atlas slope may be an explanation of the pronounced attenuation of blood flow pulsatility. The results are underlined by the theoretic consideration that in contrast to a straight vessel, a fluid running through a curved vessel generates a centrifugal force,²⁷ leading to an energy transfer from the current to the vessel wall. With regard to a physiologic pulsatile current, energy transfer from the current to the vessel wall takes place at peak systolic velocity and vice versa in the diastolic phase. The elastic vessel wall can react on the applied force with a distension during systole and a retraction during diastole, laminarizing downstream pulsatile flow appropriate to a Windkessel reservoir.^{18,28}

The results of the present study are plausible because the acquired values are consistent with low intersubject variability. The acquired values of blood velocity, PI, and RI are in good accordance with Doppler sonography measurements reported in the literature.²⁹ In the present study, a 2D-PC sequence with multidirectional velocity-encoding and high spatial resolution was chosen to accurately capture blood flow of both vertebral arteries within a single measurement. A lower temporal resolution was taken into account to achieve this.

Physiologically, the measured decrease in arterial pulsatility along the carotid siphon may be meaningful for the cerebral circulation. The brain has a low-resistance capillary bed without protective precapillary sphincters.⁷ Moreover, a physiologic dampening of arterial flow pulsatility has already been described in the anterior cerebral circulation. Here, a marked attenuation of blood flow pulsatility occurs along a short-but-curved vessel section with comparable uniformity to the Atlas slope, the carotid siphon.¹⁸

During recent years, there has been increasing evidence about the negative impact of increased arterial flow pulsatility on the brain.

Recent large collective longitudinal studies have shown that increased PI and RI correlate significantly with cerebral white matter hyperintensities.⁸ In this context, PI correlated strongest with white matter hyperintensities as radiologic correlates of microvascular disease of the evaluated parameters.⁹ Another recent study of patients with ischemic stroke showed significantly higher PI and RI in patients with lacunar stroke based on cerebral microvascular disease compared with other stroke subtypes.¹⁰ These new data are in accordance with previous studies of patients with type 2 diabetes mellitus in whom increased arterial pulsatility correlated with a higher degree of cerebral microangiopathy.^{30,31} Bateman et al³² have also shown that early vascular dementia is associated with increased blood flow pulsation.

A shortcoming of the present study is the absence of patient data. However, our intention was primarily to evaluate a potential physiologic function of the Atlas slope and to establish baseline values in terms of pulsatility changes. Shortcomings of the applied MR imaging sequence are a lower temporal resolution and slightly increased scanning time due to multidirectional velocity-encoding compared with a standard unidirectionally encoded 2D-PC

sequence. In contrast, 4D-PC-MR imaging shows even less underestimation of flow velocities compared with a 2D-PC acquisition with 3D velocity-encoding. However, a 4D-PC sequence with the necessary spatial resolution would have resulted in extensive scanning time. Nevertheless, we think that the applied technique is advantageous, if the paired cervical arteries are measured within 1 planar sequence. This advantage is underlined by the accordance of the measured values with sonography data.²⁹

CONCLUSIONS

On the basis of the observation that increased arterial pulsatility appears to harm the brain parenchyma, the measured attenuation of pulsatility along the Atlas slope seems plausible. How arterial stiffness affects the demonstrated pulsatility attenuation along the Atlas slope and whether there is a difference between healthy elderly and individuals with white matter hyperintensities are interesting questions for future study. In this context, the pulsatility attenuation may also be evaluated as a surrogate marker for white matter hyperintensities.

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